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VII-4 Change in Mean Square Radius between Ground and Excited States in Deformed Nuclei

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Nuclear rotational motion gives a few influences on the structure of nucleus.¹⁻²) One of them is the so called centrifugal stretching effect and the other is the antipairing effect. An intuitive interpretation of the former effect is that the centrifugal force stretches a nucleus and nuclear shapes change with angular momentum. Previously¹⁾ we calculated the difference of the quadrupole deformation of 2⁺ and 0⁺ states in the ground band $\delta\beta_2$ taking account of the antipairing effect. In that work only the quadrupole deformation β_2 was considered and the hexadecapole deformation β_4 was ignored. The results of our calculation showed that the sign of $\delta\beta_2$ is positive and supported the intuitive interpretation. Recently the difference of the monopole moment of 2^+ and 0^+ ground band states $\delta \langle r^2 \rangle / \langle r^2 \rangle$, the isomer shift, was systematically measured for rare-earth nuclei by using the Mössbauer effect and muonic atoms.3) An interesting fact is that the sign of $\delta \langle r^2 \rangle / \langle r^2 \rangle$ is not always positive and is negative for nuclei in the latter half of the rare-earth region. The relation between $\delta\beta_2$, $\delta\beta_4$ and $\delta \langle r^2 \rangle / \langle r^2 \rangle$ is given as follows:

$$\begin{split} \delta \langle r^2 \rangle / \langle r^2 \rangle &= \frac{5}{2\pi} \left\{ \left(\beta_2 + \frac{15}{\sqrt{98\pi}} \beta_2 \beta_4 \right) \delta \beta_2 \right. \\ &+ \left(\beta_4 + \frac{15}{7\sqrt{4\pi}} \beta_2^2 \right) \delta \beta_4 + \cdots$$

Here, $\delta\beta_2$ and $\delta\beta_4$ are the differences between the deformation parameters which give the energy minimum for the ground 0⁺ and first 2⁺ states. As the second term in the right hand side is small, the sign of $\delta\langle r^2 \rangle / \langle r^2 \rangle$ is almost determined by the first term only. In some cases $\delta\beta_2$ becomes negative. This improves the results in our previous work so as to fit the experiments. We recalculated $\delta\langle r^2 \rangle / \langle r^2 \rangle$ taking account of both the quadrupole and hexadecapole deformations. The used parameters defining single



particle level spectra are those of Gustafson *et al.*⁴⁾ The values of the deformation parameters β_2 and β_4 in the ground state coincide with those obtained by Möller.⁵⁾ The results are plotted on Fig. 1 with experimental values as a function of atomic mass number. We can see from Fig. 1 that the introduction of the hexadecapole deformation explains qualitatively the experimental tendency of the isomer shift.

References

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